

CUBE 4.3.4 – Cube Derived Metrics

Usage and syntax documentation

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The Scalasca Development Team scalasca@fz-juelich.de

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1 Introduction into Cube Derived Metrics

1.1 Introduction

With Cube 4.1.0 derived metrics are introduced and provide a powerful tool for performance data processing.

Unlike normal metrics of the cube, derived metrics do not store any data inside of the cube report, but derive their value according to an expression, formulated using CubePL (Cube Processing Language) syntax ('Syntax of CubePL').

Cube supports different kinds ('The three kinds of derived metrics') of derived metrics. Derived metric can be a child metric of any metric of cube or other derived metrics.

Derived metrics are naturally metrics with the value DOUBLE

1.2 Creation of a derived metric in Cube

Derived metrics play the very same role as a normal metric in cube, therefore one proceeds with creation of derived metrics as usual. The only difference is the specification of the CubePL expression.

1.2.1 Using the C writer

To create a derived metric in a C program, one calls cube_metric_set_← expression(...) subsequently to cube_def_met(...). Here is a code example:

```
);
cube\_metric\_set\_expression(met, \textcolor{stringliteral}{"metric::time(i)/metric::visits(e)"});
```

Derived metric specification allows to define an CubePL expression, which will be execuded only once before the actual metric expression is executed. To specify an initalization expression, one uses the call <code>cube_metric_set_init_expression(...)</code>.

Prederived metrics allow to redefine operators "+" and "-" in the aggregation formula by any user defined expression using same CubePL syntax.

Any such expression should be a formula of "arg1" and "arg2" parameters. E.g max(arg1, arg2).

To specify an expression for an aggregation operator one uses the call $cube_metric_$ $cupe_metric_$ $cupe_$ $cupe_$ cupe

1.2.2 Using the C++ library

To create a derived metric in C++ programs, one specifies the expression as the last parameter of the metric definition. This parameter can be omitted, in this case the derived metric returns always 0.

Here is a code example:

CUBE_METRIC_PREDERIVED_EXCLUSIVE defines the kind of the derived metric (see 'The three kinds of derived metrics' below).

Derived metric specification allows to define an CubePL expression, which will be execuded only once before the actual metric expression is executed. This expression is the last argument in the parameter { \${unit}}=1000; }.

Operator "+" is redefined like min (arg1, arg2).

Note, that the CubePL expression should be valid at the time of execution. It means, if there is a reference to metric, this metric should be defined before.

1.3 The three kinds of derived metrics

Cube provides an API to calculate different inclusive and exclusive values aggregated over different dimensions.

In the context of derived metrics it is sometimes useful, when evaluation of the expression is done after the aggregation of the metrics in the expression, sometimes it is needed to aggregate values of the derived metrics.

Therefor Cube provides three kinds of derived metrics:

1. **Prederived exclusive metric** - metric, which value of which expression is observed as "being stored" inside of cube report and it behaves as a usual exclusive (along call tree) metric.

One specifies this type of metric using constant

```
CUBE_METRIC_PREDERIVED_EXCLUSIVE
```

For this metric one can redefine only operator "+". Operator "-" will be ignored.

2. **Prederived inclusive metric** - metric, which value of which expression is observed as "being stored" inside of cube report and it behaves as a usual inclusive (along call tree) metric.

One specifies this type of metric using constant

```
CUBE_METRIC_PREDERIVED_INCLUSIVE
```

For this metric one can redefine both operators, "+" and "-".

3. **Postderived metric** - metric, which expression evaluated only after metrics, which were used inside of the expression, get aggregated according to the aggregation context (along system tree or along call tree).

If expression doesn't contain references to another metrics, no aggregation is done. In this case the expression gets calculated and its value returned.

One specifies this type of metric using constant

```
CUBE_METRIC_POSTDERIVE
```

This metric doesn't allow to redefine anyoperators, because calculation of this metric is performed AFTER aggregation within another metric.

2 Syntax of CubePL

2.1 Syntax step by step

This chapter introduced the CubePL syntax of the most common programming structures.

2.1.1 Expressions

2.1.1.1 Constants

Any constant expression is an expression. eg. 123.0, "someString"

2.1.1.2 Arithmetical Expressions

Common mathematical notation of an arithmetical expression is valid in CubePL. Any arithmetical expression is an expression. eg. 123.0 + 23.6, sin(23)

2.1.1.3 Boolean Expressions

Common literal notation of a boolean expression is valid in CubePL. Any boolean expression is an expression.

```
[expression] or|and|xor [expression]
or
not [expression]
```

Any expression can be a term of a boolean expression. Non zero value is observed as TRUE, zero value is FALSE.

2.1.1.4 Function call expressions

Function calls have the following syntax:

```
name ( [expression] )
```

2.1.2 Lambda function (In-place function definition)

To define a function in-place, one uses the following syntax:

```
\{
   [statement];
   [statement];
   ...
   \textcolor{keywordflow}{return} [expression];
\}
```

In-place definition of a function is an expression. It means, it can appear everywhere, where one can use an expression.

2.1.3 Control structures

Control structures like if-else or while are statements.

2.1.3.1 Condition IF-ELSE

One can execute series of statements under a condition using the short form of the if statement:

```
\textcolor{keywordflow}{if} ( condition )
\{
  [statement];
  [statement];
  ...
\}
```

or full form with else:

```
\textcolor{keywordflow}{if} ( condition )
\{
    [statement];
    [statement];
    ...
\}
\textcolor{keywordflow}{else}
\{
    [statement];
    [statement];
    [statement];
    ...
\}
```

condition is a boolean expression

2.1.3.2 Loop WHILE

One can execute a series of statements as long as a condition is true using the while statement:

```
\textcolor{keywordflow}{while} ( condition )
\{
  [statement];
  [statement];
  ...
\}
```

Sequence of statements will be executed till condition is not fulfilled, max 1000000000 times.

2.1.4 Variables

CubePL allows to work with memory, by using variables. All variables are multi-typed:

- In string context value of a numeric variable is presented in string format.
- In numerical context a string variable is converted to its numerical representation, if possible. Otherwise it is 0.

All variables are arrays. Indexless access to the variable assummes mutually index value 0.

2.1.4.1 User defined Variables

The user can define a variable using the syntax:

```
$\{ name \} = [expression];

or

$\{ name \}[index] = [expression];
```

Currently its name is a fixed string of characters. In later versions of CubePL it will allow any expression.

Example of a string context:

```
$\{name\} seq \textcolor{stringliteral}{"STRING"}
```

Example of a numeric context:

```
\eta = 0.34
```

Example of an array access to the variable:

```
\alpha \ {name\}[ $\{i\} ] >= 0.34
```

Access to the variable is an expression.

Index for the access to the value is also an expression.

2.1.4.2 Predefined Variables

Cube provides a set of predefined variables for every calculation, which values are independend. Following predefined variables do contain the general information about the cube:

Predefined variable	Explanation
cube::#mirrors	Number of mirrors in cube file
cube::#metrics	Number of metrics in cube file
cube::#root::metrics	Number of root metrics in cube file
cube::#regions	Number of regions in cube file
cube::#callpaths	Number of call paths in cube file
cube::#root::callpaths	Number of root call paths
cube::#locations	Number of locations in cube file
cube::#locations::void	Number of void locations in cube file
cube::#locations::nonvoid	Number of nonvoid locations in cube file
cube::#locationgroups	Number of location groups in cube file
cube::#locationgroups::void	Number of void location groups in cube
	file
cube::#locationgroups::nonvoid	Number of nonvoid location groups in
	cube file
cube::#stns	Number of system tree nodes in cube file
cube::#rootstns	Number of root system tree nodes in
	cube file
cube::filename	Name of the cube file

CubePL engine defines a set of variables, which do depend on an index, their "id". Using call sizeof(...) one can run over them and inspect within CubePL expression.

cube::metric::unit::nameUnique name of the metriccube::metric::disp::nameDisplay name of the metriccube::metric::urlURL of the documentaticube::metric::descriptionDescription of the metriccube::metric::dtypeData type of the metriccube::metric::uomUnit of measurement ofcube::metric::expressionCubePL expression of thecube::metric::initexpressionCubePL initialisation ex	tric on of the metric c the metric ne metric pression of the
cube::metric::urlURL of the documentaticube::metric::descriptionDescription of the metriccube::metric::dtypeData type of the metriccube::metric::uomUnit of measurement ofcube::metric::expressionCubePL expression of the	the metric ne metric pression of the
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	pression of the
cube::metric::initexpression	_
metric	natui a
cube::metric::parentd::id ID of the parent of the m	101177'
cube::metric::#children Number of children in the	
cubemetric#emidren	ic mearc
cube::callpath::mod Module of the call path	
cube::callpath::line File line of the call path	
cube::calleeid ID of the callee region	
cube::callpath::#children Number of children in the	-
cube::callpath::parent::id ID of the parent callpath	1
cube::region::name Name of the region	
cube::region::mangled::name Mangled name of the reg	
cube::region::paradigm Name of the paradigm of	f the region
cube::region::role Name of the role the reg	ion is playing
within the paradigm	
cube::region::url URL with the description	n of the region of
the call path	
cube::region::description Description of the region	
cube::region::mod Module of the region of	
cube::region::begin::line Begin line of the region	of the call path
cube::region::end::line End line of the region of	the call path
cube::stn::name	node
cube::stn::class Class of the system tree	
cube::stn::description Description of the system	
cube::stn::#children Number of children (oth	
nodes) of the system tree	•
cube::stn::#locationgroups Number of location group	
tree node	- •
cube::stn::parent::id ID (among all system tre	ee nodes) of the
parent of the system tree	
cube::stn::parent::sysid ID (global) of the parent	
tree node	-

cube::locationgroup::name	Name of the location group
cube::locationgroup::rank	Rank of the location group
cube::locationgroup::type	Type of the location group
cube::locationgroup::void	Is the this location group void?
cube::locationgroup::#locations	Number of locations of the location
	group
cube::locationgroup::parent::id	ID (amoung all system tree nodes) of the
	parent system tree node
cube::locationgroup::parent::sysid	ID (global) of the parent system tree
	node

cube::location::name	Name of the location
cube::location::rank	Rank of the location
cube::location::type	Type of the location
cube::location::void	Is the this location void?
cube::location::parent::id	ID (among all location groups) of the
	parent location group
cube::location::parent::sysid	ID (global) of the parent location group

CubePL engine sets a series of context sensetive variables, which value depends on the paramaters, for which the derived metric is being calculated. Their value can be used to refer to the values of context insensitive variables described above:

calculation::metric::id	ID of the metric, being calculated	
calculation::callpath::id	ID of the callpath, for what is the metric	
	being calculated	
calculation::region::id	ID of the region, for what is the metric	
	being calculated	
calculation::sysres::id	ID (global) if the sysem resource, for	
	what is the metric being calculated	
calculation::sysres::kind	Type of the system element:	
	• 0 = unknown	
	• 5 = system tree node	
	• 6 = location group	
	• 7 = location	

2.1.5 Different ways to refer an another metric

2.1.5.1 Context sensitive reference to another metric

To use values of another metric in the same calculation context, one uses syntax:

```
metric::[uniq\_name]( modificator, modificator )

or

metric::[uniq\_name]( modificator)

or

metric::[uniq\_name]()
```

There are three version of this call:

- 1. with two arguments (call path and system);
- 2. with one argument (call path);
- 3. with no argument(an arguments takes as '*').

modificator specifies flavor of the calculation: i - inclusive, e - exclusive, * - same like in calculation context.

Metric reference is an expression.

2.1.5.2 Context insensitive reference to another metric

To use values of another metric in the some fixed calculation context (e.g. aggregated over threads), one uses syntax:

```
metric::fixed::[uniq\_name]( modificator, modificator )

or

metric::fixed::[uniq\_name]( modificator)

or

metric::fixed::[uniq\_name]()
```

There are three version of this call:

- 1. with two arguments (call path and system);
- 2. with one argument (call path);
- 3. with no argument(an arguments takes as '*').

modificator specifies flavor of the calculation: i - inclusive, e - exclusive, * - same like in calculation context.

Metric reference is an expression.

2.1.5.3 Direct reference to another metric

To use values of another metric with an specific call path id and system resource id (!), one uses syntax:

```
metric::call::[uniq\_name]( callpath id, modificator, sysres id, modificator )

or

metric::call::[uniq\_name]( callpath id, modificator )
```

There are two version of this call:

- 1. with four arguments (call path and system); Only callculation of an inclusive or exclusive value is performed
- 2. with one argument (call path); Aggragation over system tree is performed additionally to the calculation of the inclisive or exclusive value for the calltree id

modificator specifies flavor of the calculation: i - inclusive, e - exclusive.

Metric reference is an expression.

Note that "sysres id" is a global identificator and can be refered using \${calculation← ::sysres::id}.

2.1.5.4 Definition of an encapsulated calculation within CubePL expression using metrics of Cube.

One special mechanis of CubePL processing engine allows some level of calculation separation. A derived metric can be created within another CubePL expression. Such "ghost" metric gets its name and properties and exists inside of the cube object as a casual metric. Only difference to the casual metric is in the fact that ghost metric is not visible in GUI and tools and is not stored inside of the metric tree of the cube file.

One can refer such metric as a casual metric using metric references (see 'Context sensitive reference to another metric', 'Context insensitive reference to another metric' and 'Direct reference to another metric').

Example for definition of such metric:

```
\};
\};
\textcolor{keywordflow}{return} $\{\textcolor{keywordflow}{return}\};
\}
>>;
$\{visitors\} = metric::fixed::nvisitors(e);
where
cube::metric::prederived::nvisitors(e)
```

gives a type (prederives, exclusive) and unique name (nvisitors) of this metric. Unique name is used then later to refer to this metric via

```
$\{visitors\} = metric::fixed::nvisitors(e);
```

There are kinds of metrics, which can be defined on such manner:

- 1. cube::metric::prederived::name(e) An exclusive prederived metric with the name name;
- 2. cube::metric::prederived::name(i) An inclusive prederived metric with the name name;
- 3. cube::metric::postderived::name A postderived metric with the name name.

Notice that once the metric with some unique name created it exists whole lifetime of the cube object. Therefore one can refer to some somewhere previously defined ghost metric from any following it CubePL expressions.

Ghost Metric definition is a statement.

2.1.5.5 Definition of an initialization expression for ghost metrics within CubePL expression.

One can specify within of a CubePL expression an initialisation phase for previously created ghost metric. For that purpose one uses expression cube::init::metric: : [name]. Notice that named metric should be know by the moment of compilation of the CubePL expression.

Example for definition of such metric:

```
cube::init::metric::init::nvisitors
<<
    \{
      global(nvisitors);
    \}
>>;
```

where

```
cube::init::metric::nvisitors
```

uses an unique name (nvisitors) of the metric.

Definition of the initialisation phase of a metric is a statement.

2.1.5.6 Definition of an initialization expression for ghost metrics within CubePL expression.

One can specify within of a CubePL expression an aggregation operator "+" or "" for previously created ghost metric. For that purpose one uses expression cube
::metric::plus::[name] or cube::metric::minus::[name]. Notice that named
metric should be know by the moment of compilation of the CubePL expression.

Example for definition of such metric:

```
cube::init::metric::plus::nvisitors
<<
max( arg1, arg2)
>>;

or

cube::init::metric::minus::nvisitors
<<
min( arg1, arg2)
>>;

where

cube::init::metric:plus::nvisitors
or

cube::init::metric:plus::nvisitors
```

uses an unique name (nvisitors) of the metric.

Definition of the initialisation phase of a metric is a statement.

2.2 Grammar of CubePL

Here will be a full grammar of CubePL expressions (later).

3	Reference	of	Cub	PI
J		VI	Vun	CI L

3.1 Supported calls in CubePL

Here is the table of currently supported calls in CubePL:

Operation	Explanation
123.34	a numerical constant
"STRING"	a string constant
-X	negative value of x
()	grouping (priority)
	absolute value
+-/*	arithmetical operations
$A^{\wedge}x$	A in power of x
> < >= <= != ==	numerical comparison
and or xor not	boolean operations
eq	string comparison
seq	case insensitive string comparison
=~ /expression/	matching of regular expression
$\sin(x)\cos(x) \sin(x) \cos(x) \tan(x) \cot(x)$	trigonometrical functions
atan(x) acot(x)	
ln(x)	natural logarithm of x
exp(x)	natural exponent of x
sqrt(x)	square root value of x
random(x)	random number from 0 to x
pos(x)	returns x, if $x>$, or 0
neg(x)	returns x, if $x<0$, or 0
sgn(x)	returns -1, if $x<0$, 0 if x is 0 and 1 is $x>0$
abs(x)	returns absolut value
ceil(x)	returns smallest integer value, which is
	bigger than x
floor(x)	returns biggest integer value, which is
	smaller than x
min(x,y)	returns smaller value of x and y
max(x,y)	returns bigger value of x and y
uppercase(x)	returns uppercase version of x
lowercase(x)	returns lowercase version of x
env("x")	returns a value of the environment
	variable x

local(var)	Declares (to compile time) a variable <i>var</i>
alahal(yan)	as local. It cannot be redeclared later
global(var)	Declares (to compile time) a variable <i>var</i>
Φ()	as global. It cannot be redeclared later
\${var}	Oth element of the variable with name
Φ(), ,	var
\${var}[x]	x-th element of the variable with name
	var
sizeof(var)	number of elements in the variable <i>var</i>
defined(var)	returns true (1), if the variable <i>var</i> is
	defined, otherwise it returns false (0)
metric::[uniq_name](i e *, i e *)	context sensetive value of metric
	uniq_name
metric::context::[uniq_name](i e *, i e *)	context sensetive value of metric
	uniq_name
metric::fixed::[uniq_name](i e *, i e *)	context independend value of metric
	uniq_name
metric::call::[uniq_name](c_id, i e *,	value of metric <i>uniq_name</i> for the call
$ \mathbf{s_id}, \mathbf{i} \mathbf{e} *)$	path with id c_id and system resource
	with an id <i>s_id</i>
cube::metric::set::[uniq_name]("X",	sets a property X of a metric uniq_name
"Y")	to value Y. Corrently supported are only
	"value" with value "VOID" or else
cube::metric::get::[uniq_name]("X")	returns a property X of a metric
	<i>uniq_name</i> . Corrently supported are
	7 11
	1. <i>unique name</i> - returns unique name
	of a metric uniq_name
	2 1: 1
	2. <i>display name</i> - returns display
	name of a metric uniq_name
	3. <i>uom</i> - returns unit of measurement
	of a metric <i>uniq_name</i>
	or a meane uniq_name
	4. <i>dtype</i> - returns data type of a
	metric <i>uniq_name</i> as a string
	5. <i>url</i> - returns url of online help for
	the metric <i>uniq_name</i>
	6. <i>description</i> - returns description of
	a metric <i>uniq_name</i>
	7. <i>value</i> - returns property "value" for
	the metric <i>uniq_name</i> . Its value
	"VOID" deactivates metric and it
	returns always a zero.
	ictums aiways a zero.
	17

4 Examples of CubePL expressions

4.1 Simple Examples

1. Calculation of an arithmetical expression

```
123.4 + 234 - ( 23)^2
```

2. Calculation of an arithmetical expression with different functions

```
\sin(23 + \ln(12))
```

4.2 Complex Examples

4.2.1 Different made-up expressions

1. Definition of a constant function

```
\{ \textcolor{keywordflow}{return} 24; \}
```

2. Definition of a more complex function

```
\{ \textcolor{keywordflow}{return} sin (\{ \textcolor{keywordflow}{return} 1; \}); \}
```

3. Definition of a function with an access to one variable

```
{\{a\}}=123; \text{ textcolor}\{\text{keywordflow}\}\{\text{return} \ \{a\}\}; \ }
```

4. Definition of a function with a control structure

```
\{
    $\{a\}=metric::visits();
    $\{b\}=0;
    \textcolor{keywordflow}{if} ($\{a\}>100)
    \{ $\{b\}=metric::time(); \};
\textcolor{keywordflow}{return} $\{b\};
\}
```

5. Definition of a function with a loop structure

```
\{
    $\{a\}=0; $\{b\}=0;
\textcolor{keywordflow}{while} ($\{a\}<123)
\{
    $\{b\}=$\{b\}+metric::time();
    $\{a\}=$\{a\}+1;
\};</pre>
```

```
\textcolor{keywordflow}{return} $\{b\};
\}
```

6. Definition of a function with a access to predefined variable

```
\{
    $\{a\}=0;
   \textcolor{keywordflow}{if} ($\{calculation::region::name\}[$\{calculation::callpath::id\}]
    \{
        $\{a\}=metric::time();
    \};
   \textcolor{keywordflow}{return} $\{a\};
   \\}
```

4.2.2 Special metrics of Scalasca

1. Calculation of an average runtime of a call path (Kenobi metric, postderived)

```
metric::time(i)/metric::visits(e)
```

- 2. Calculation of the time, spend in MPI synchronization calls
 - a) (initialization)

```
\ {
   global(mpi\_synchronization);
   $\{i\}=0;
   \textcolor{keywordflow}{while}( $\{i\} < $\{cube::#callpaths\} )</pre>
      {\rm pi}_synchronization} {\{i\}} = 0;
      $\{regionid\} = $\{cube::callpath::calleeid\}[$\{i\}];
      \textcolor{keywordflow}{if} (
          ($\{cube::region::paradigm\}[ $\{regionid\} ] seq \textcolor{stringliteral}{
          and
          ($\{cube::region::name\}[$\{regionid\}] seq \textcolor{stringliteral}{"mpi\
          ($\{cube::region::name\}[$\{regionid\}] seq \textcolor{stringliteral}{"mpi\
          ($\{cube::region::name\}[$\{regionid\}] seq \textcolor{stringliteral}{"mpi\
          ($\{cube::region::name\}[$\{regionid\} ] seq \textcolor{stringliteral}{"mpi\
          ($\{cube::region::name\}[$\{regionid\}] seq \textcolor{stringliteral}{"mpi\
          \label{lem:color} $$ \sin me\] [\$\frequency] = seq \textcolor{stringliteral}{"mpi} $$
          )
      \{
```

 ${\rm pi}_synchronization} {\{i\}} = 1;$

- 3. Calculation of the Computational load imbalance (single participant)
 - NO EXAMPLE YET -